

# Shear instabilities in the context of liquid atomization

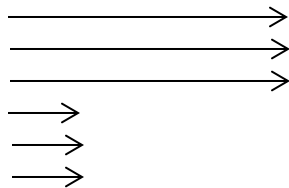
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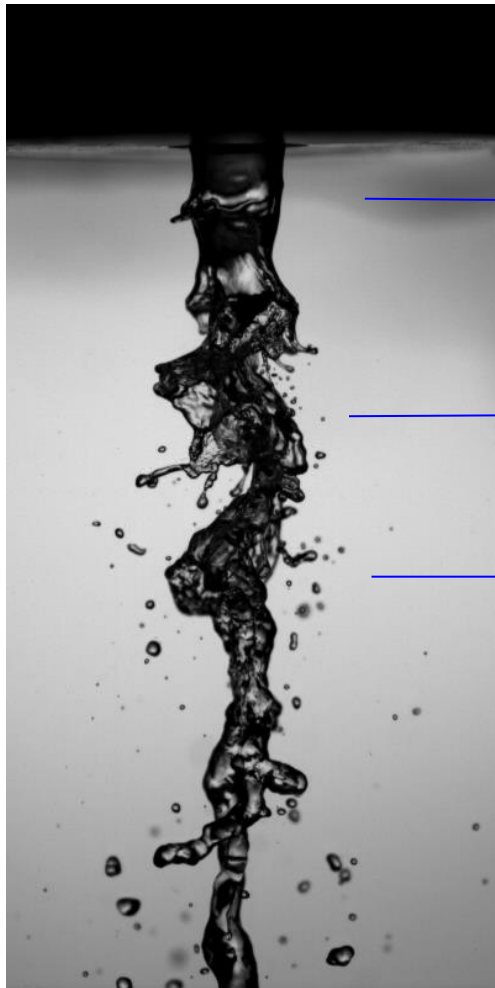
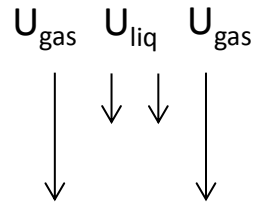
Gas  
Liquid

A diagram showing flow directions for gas and liquid. Three horizontal arrows point to the right, labeled 'Gas'. Below them, three horizontal arrows also point to the right, labeled 'Liquid'.

$U_G=22 \text{ m/s}$ ,  $U_L=0,42 \text{ m/s}$   
*L. Raynal, 1997*

# Liquid atomization

Successive mechanisms in spray formation

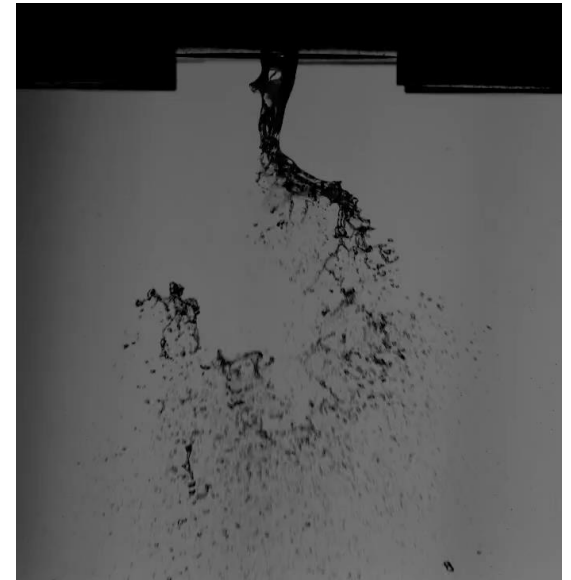


Longitudinal shear instability

Transversal instability:  
Ligament formation

Droplet formation

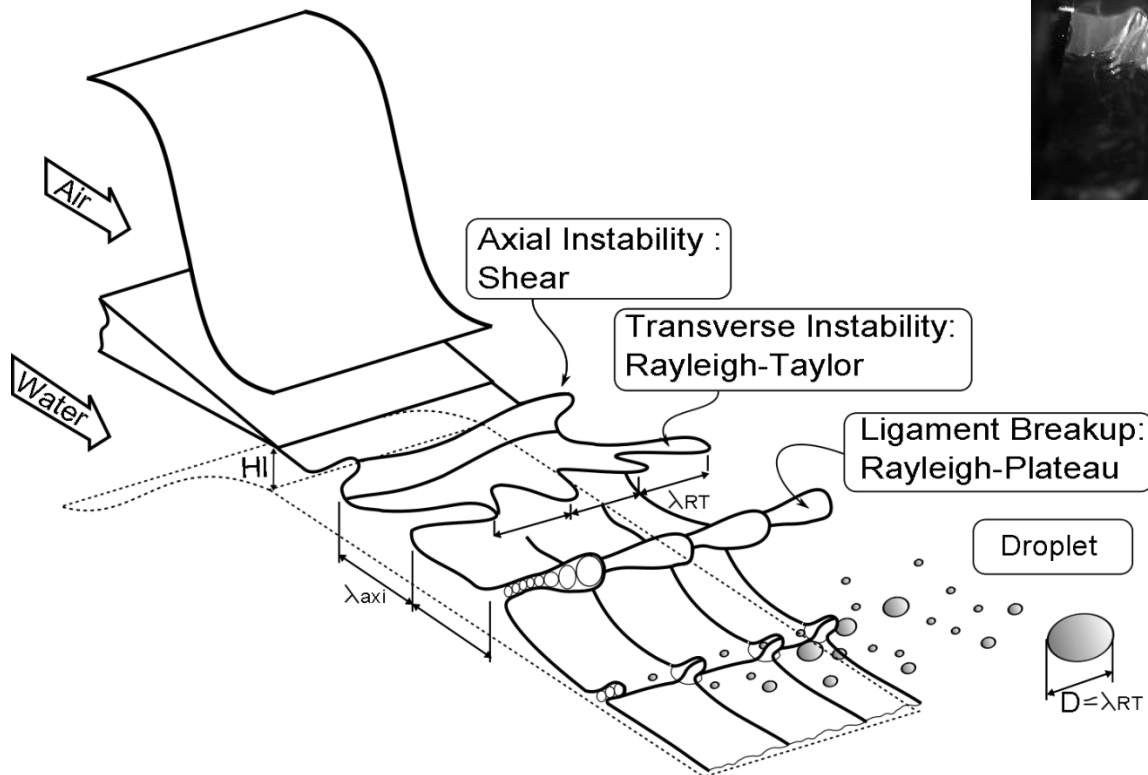
Flapping instability



# Shear instability

Thesis of Sylvain Marty

## Mixing layer configuration



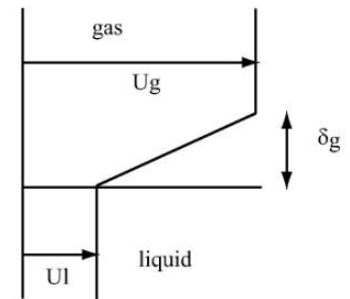
# 1. Mechanism?

- Raynal (1997) and Marmottant & Villermaux (JFM 2004):

Simple temporal **inviscid** stability analysis accounts for experimental scaling of wavelength/frequency:

$$\lambda \sim (\rho_l/\rho_g)^{1/2}\delta_g \quad \text{and} \quad f \sim (\rho_g/\rho_l)U_g/\delta_g$$

Basically: 
$$\frac{d(\text{ec})}{dt} = \rho_g u_i u_j D_{ij}$$
$$\rho_l u^2 \omega = \rho_g u^2 U_g / \delta_g$$



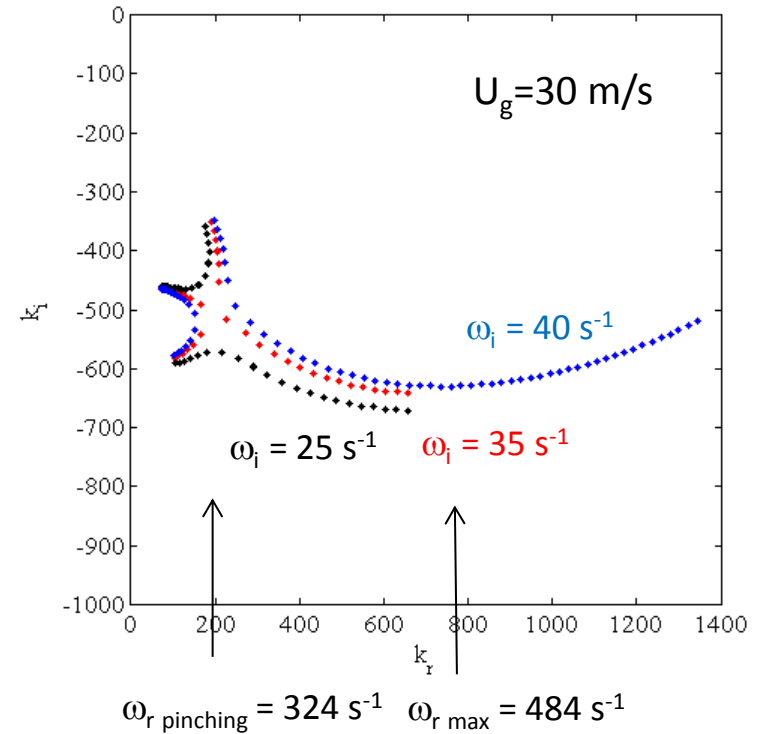
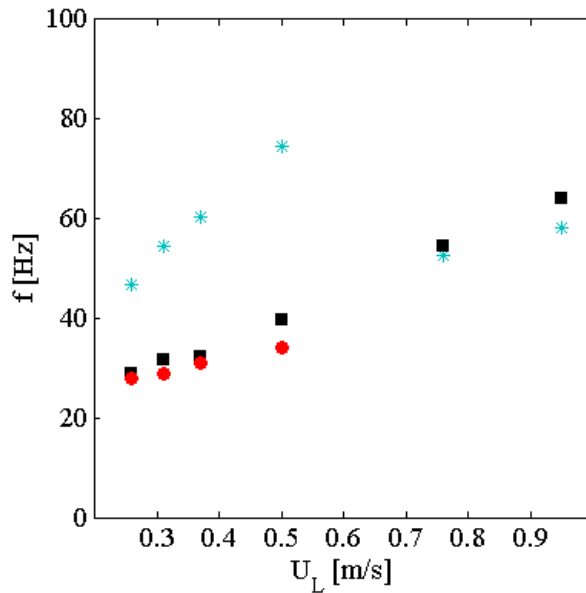
- Temporal viscous stability analysis fails miserably (wrong  $f$ ,  $\lambda$ , velocity etc): why does **simpler inviscid approach** succeed in the 1<sup>st</sup> place??

**Nature of instability: inviscid or viscous??**

# Effect of confinement

- Inclusion of finite liquid thickness in spatio-temporal analysis:

⇒ Collision with **confinement branch!!!**



**Reduction in frequency!**

■ : experiments

● : Prediction when confinement is included

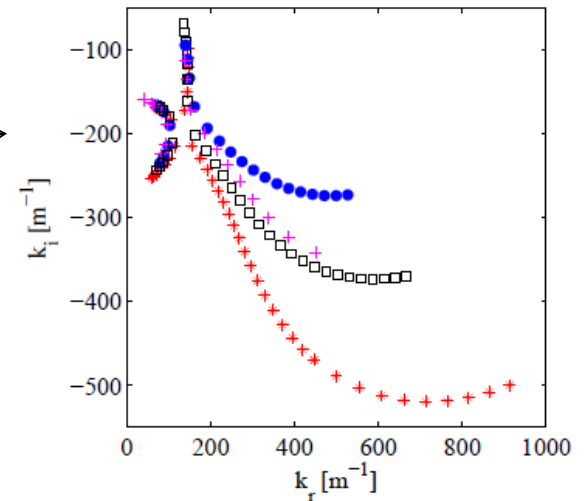
\* : prediction of Otto et al (2013)

# Inviscid vs viscous

Though shear mode is indeed viscous at  $k_{i_{\max}}$

- **Energy budget at pinch point** shows that  
(work of Reynolds stresses in gas)  $\gg$  (work of viscous stresses at interface)

- Pinch point location unaffected by change in viscosity (down to  $\nu/100$ )



- Interpretation: “Resonance” due to confinement triggers instability in a range of  $k$  where **mechanism is inviscid!**
- Justifies relevance of **simplified inviscid approach**

## 2. Impact of turbulence on shear instability?

- Reproducibility issues in the mixing layer experiment: additional parameter?
- Experimental evidence that frequency of the shear instability not only depends on **mean values**, but also on **intensity of velocity fluctuations** in gas stream
- Experiment to quantify this?



# Forcing of turbulence

1) Passive forcing (obstruction of varying height  $H$ )

Forcing produces same mean velocity profile, but differing turbulence intensity profiles.

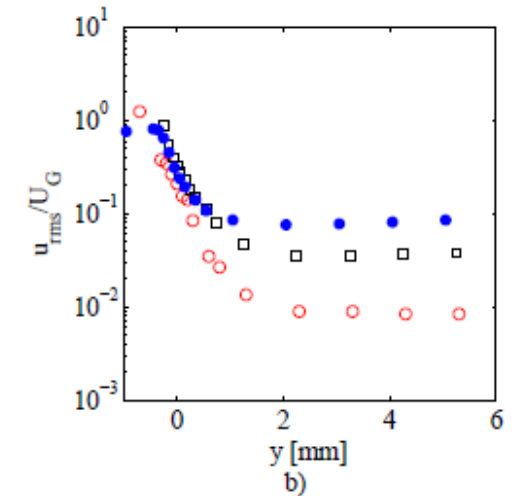
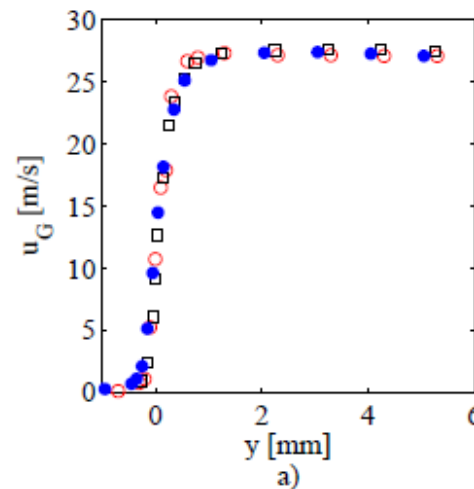
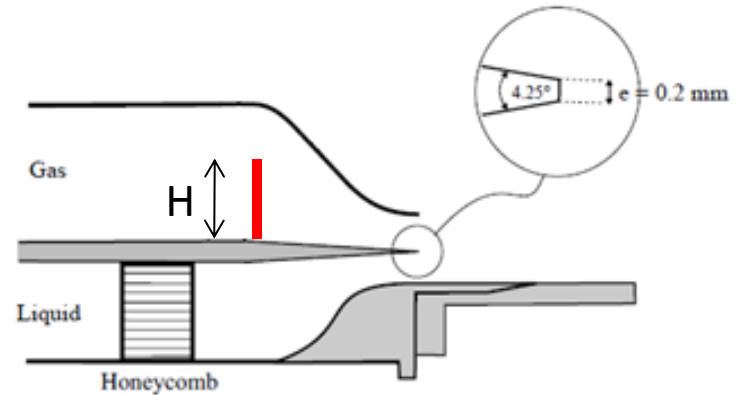
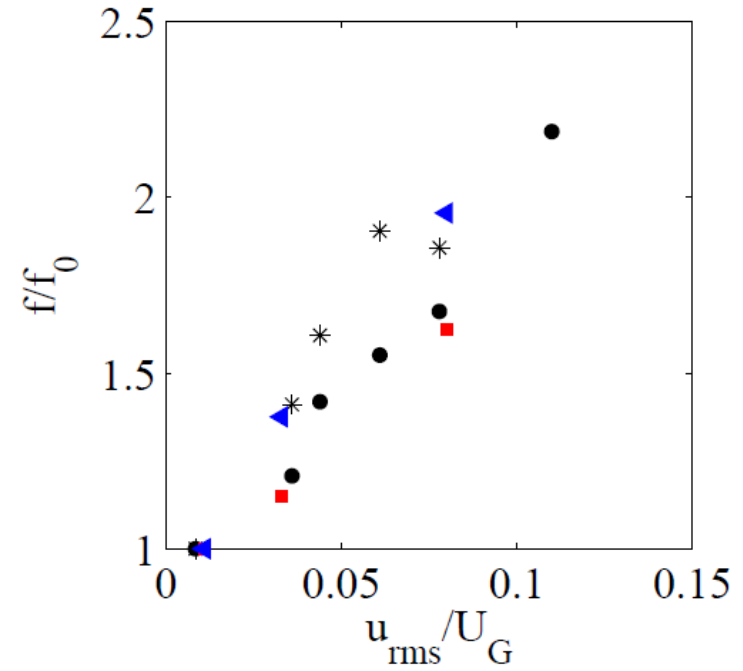
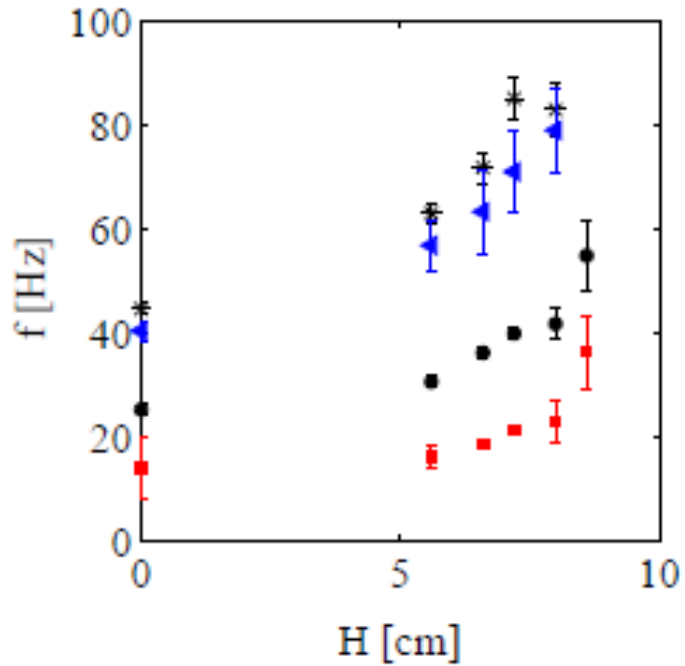


FIG. 3. (color online) Hot-wire velocity profiles for  $U_G = 27$  m/s and varying obstruction heights  $H$ :  $\circ$ :  $H = 0$  ;  $\square$ :  $H = 5.6$  cm ;  $\bullet$ :  $H = 8$  cm ; a) Mean velocity profile. b) Turbulence intensity  $u_{rms}/U_G$ .

# Forcing of turbulence

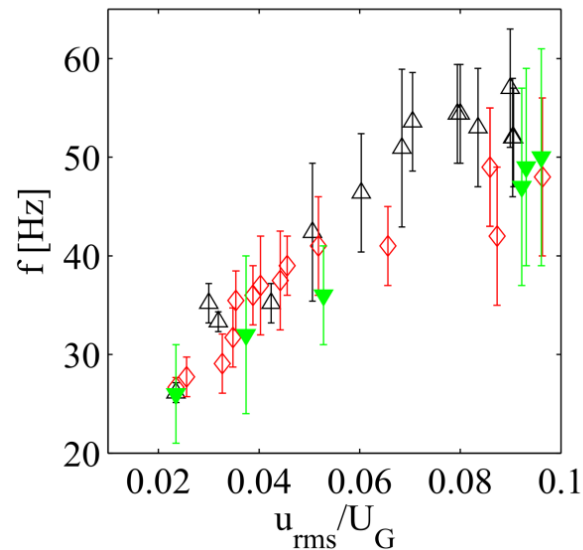
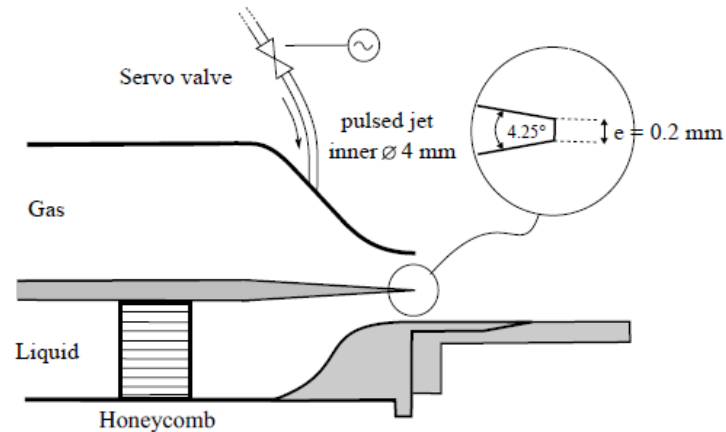


- $U_G = 27$  m/s     $U_L = 0.28$  m/s
- $U_G = 17.5$  m/s     $U_L = 0.28$  m/s
- ◀  $U_G = 40$  m/s     $U_L = 0.28$  m/s
- \*  $U_G = 27$  m/s     $U_L = 0.95$  m/s

Frequency increases with height of obstacle/turbulence intensity

# Forcing of turbulence

2) Pulsed jet method →



$U_G = 27$  m/s  $U_L = 0.28$  m/s and  
pulsed jet forcing at:

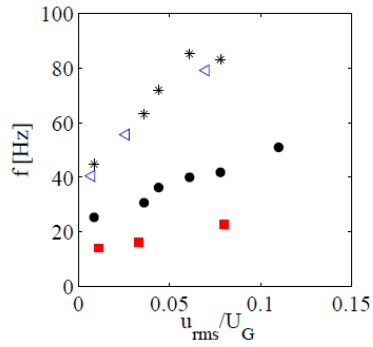
▼  $f = 17$  Hz

△  $f = 34$  Hz

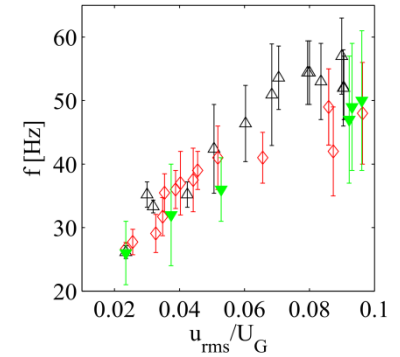
◇  $f = 70$  Hz

Frequency increases with turbulence intensity whatever the forcing method

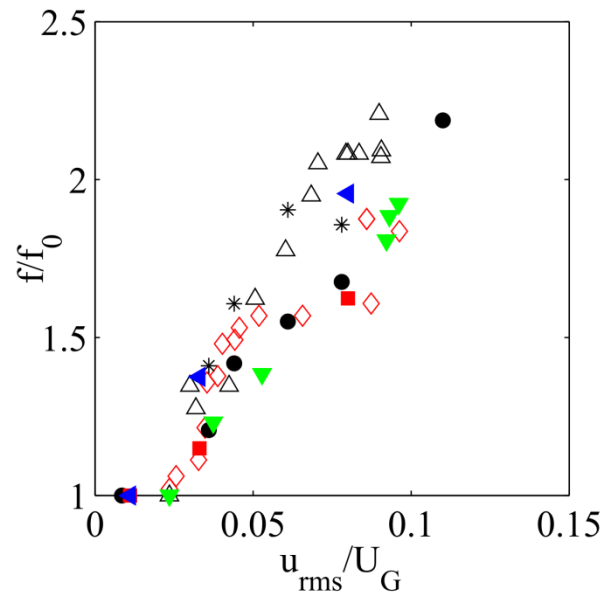
# Forcing of turbulence



Obstacle



Pulsed jet



- All data collapse when plotted as a function of  $u'/U_G$
- Independent of  $U_G$ ,  $U_L$  and forcing method

# Impact on wavelength



$u'/U = 2.3\%$   
 $f = 26\text{Hz}$  and  $\lambda \sim 3.4\text{ cm}$



$u'/U = 9\%$   
 $f = 53\text{Hz}$  and  $\lambda \sim 1.6\text{ cm}$

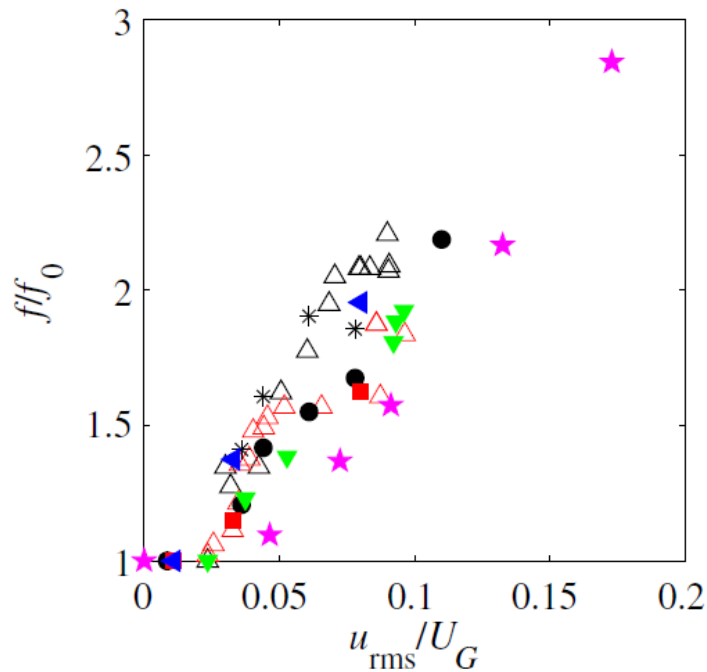
- Wavelength decreases with turbulence intensity

- Wave velocity  $\lambda f \approx \text{constant} \approx \frac{\sqrt{\rho_G} U_G + \sqrt{\rho_L} U_L}{\sqrt{\rho_G} + \sqrt{\rho_L}}$  (Dimotakis 1986)

# Stability analysis?

Assumption: turbulent intensity modelled via **Newtonian eddy viscosity**, and injected in spatiotemporal stability analysis:

$$\rho u_{\text{rms}}^2 = \mu_{\text{g turb}} U_{\text{g}} / \delta_{\text{g}} \quad \rightarrow \quad u_{\text{rms}} / U_{\text{g}} = \sqrt{\frac{\nu_{\text{g turb}}}{U_{\text{g}} \delta_{\text{g}}}}$$



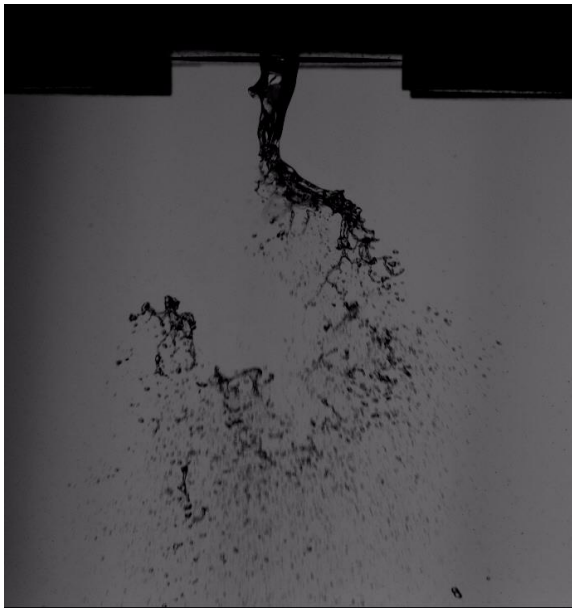
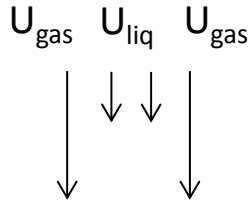
★ : stability analysis prediction with eddy viscosity

All other symbols: experimental data

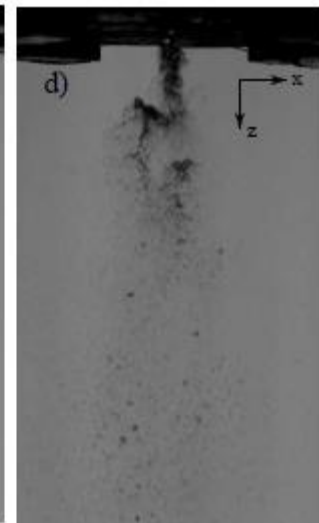
*Matas et al, PRL 2015*

# 3. Flapping instability

*Thesis of Antoine Delon (co-adv. with A. Cartellier)*



$U_{\text{gas}} = 26 \text{ m/s}$

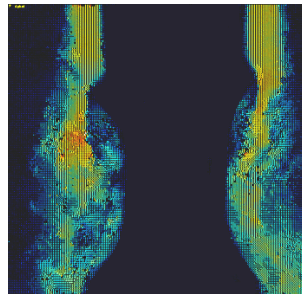


$U_{\text{gas}} = 98 \text{ m/s}$

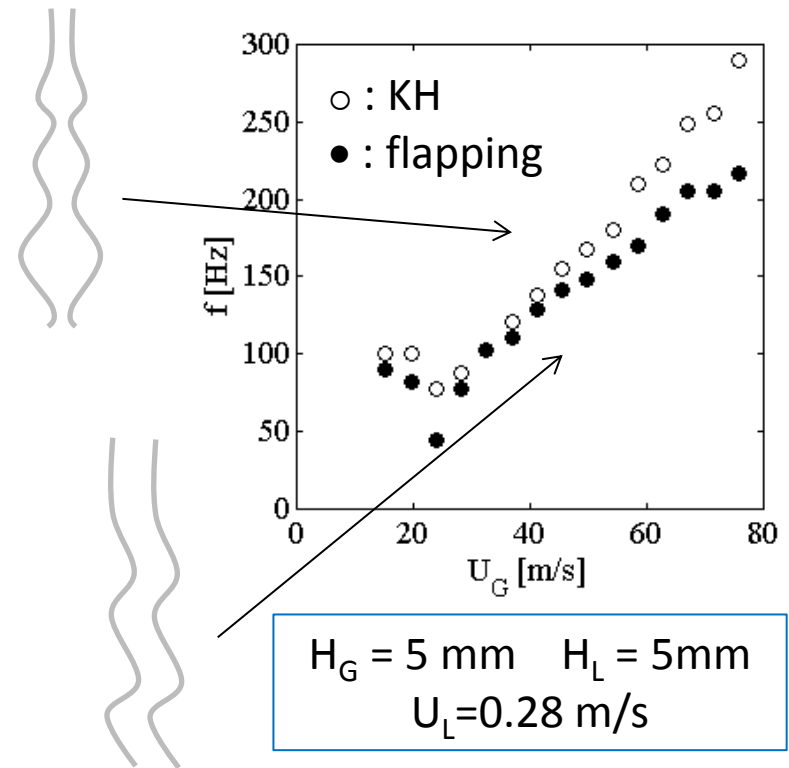
Instability present over wide range of velocities

# Frequency of flapping instability

- Capture of jet via image processing → break-up length, amplitude, frequency for several geometries
- Flapping frequency **close to** but **smaller than** axisymmetric KH waves frequency



*PIV*

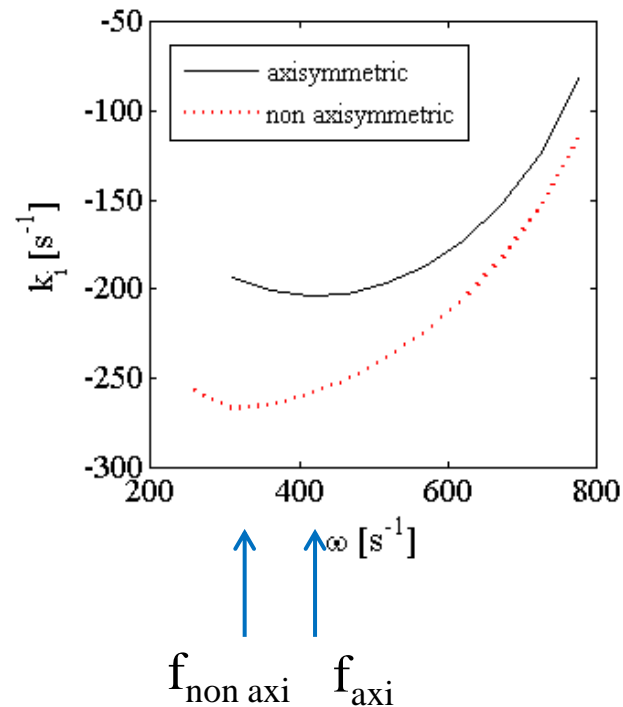
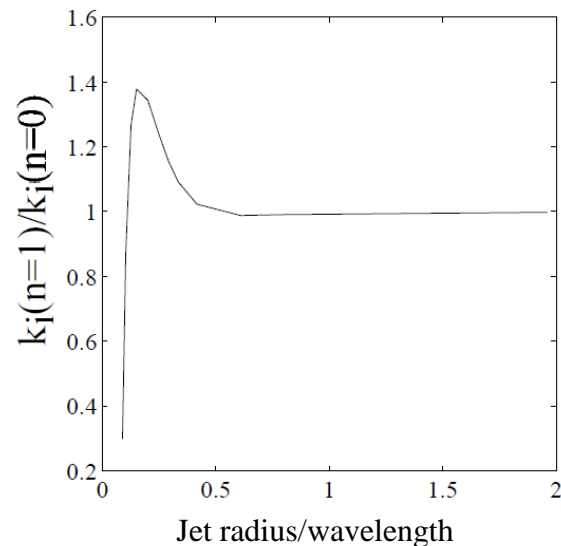


Mechanism: shear instability waves  $\Rightarrow$  vortices  
 $\Rightarrow$  **distortion of liquid jet**



# Stability of non axisymmetric modes?

- Stability of non axisymmetric ( $n=1$ ) modes investigated within inviscid hypothesis



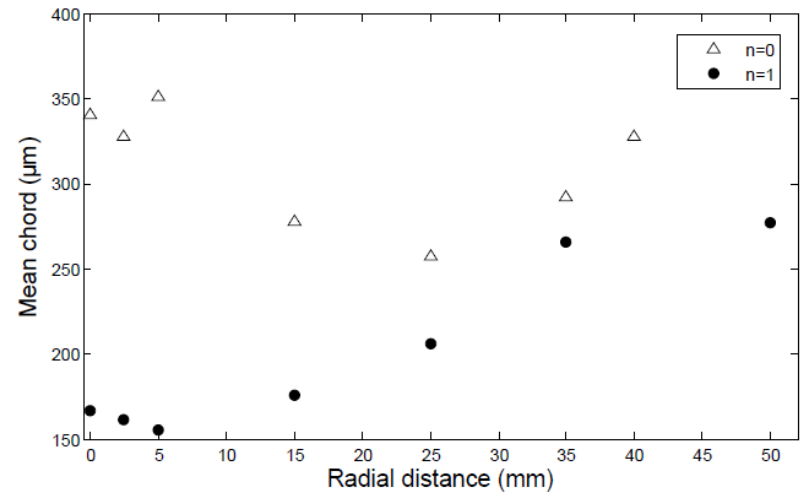
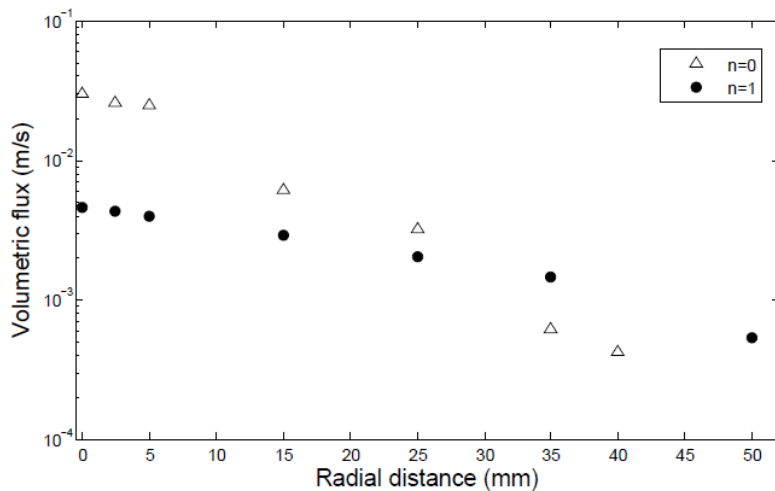
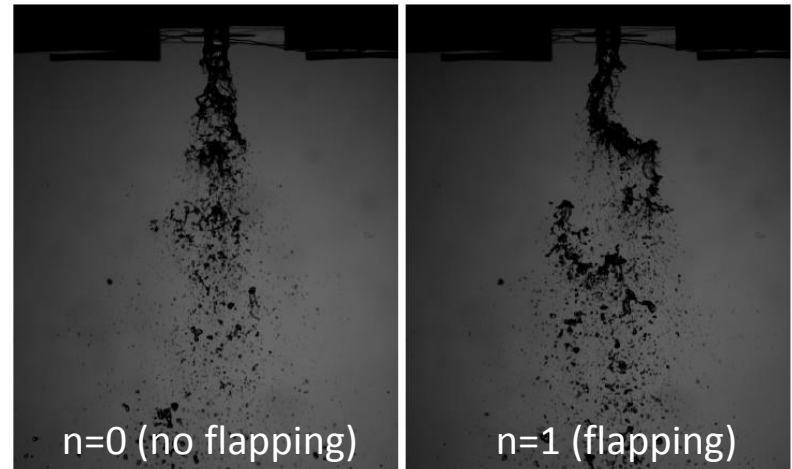
$H_G = 5 \text{ mm}$   
 $H_L = 5 \text{ mm}$   
 $U_L = 0.28 \text{ m/s}$   
 $U_G = 24 \text{ m/s}$

- Helical modes predicted to be **more unstable** than axisymmetric ones and associated frequency **20% smaller**

→ Good agreement with experiments!

# Impact on spray

Modification of velocity profile in injector →  
forcing of flapping at fixed  $U_G$  and  $U_L$



**Optical probe** measurements: Liquid redistributed differently when flapping is present: small droplets near axis, large droplets in periphery

# Further atomization configurations

- Assisted atomization of a **two-phase jet**:



- Atomization of a jet of FC-72 injected in a depressurized reservoir ( $P=5$  mbars):



- Rapid depressurization of a liquid: entrainment of FC-72 by its own vapour

