
Isotropy recovery in rotating-stratified turbulence: the role of Ozmidov and Hopfinger scales.

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Abstract

In rotating-stratified flows, two characteristic time scales, namely the BV frequency N and the Coriolis parameter f , are driving the scale of transition from isotropy to anisotropy in homogeneous turbulence. Introducing the turbulent dissipation rate ϵ , two length scales can be obtained, namely the Ozmidov length scale [1] $L_o = (\epsilon/N^3)^{1/2}$ and the Hopfinger length scale [2] $L_h = (\epsilon/f^3)^{1/2}$. Note that the Hopfinger length scale is often called the Zeman length scale [3], but was first introduced by Mory and Hopfinger in 1985 [2]. L_o and L_h compare the relative effects of inertia and of the buoyancy force or of the Coriolis force respectively, and thus quantify the rise of anisotropy in different scale ranges: at large scales (larger than L_o or L_h) the anisotropy due to strong stratification or strong rotation is dominant, whereas at small scales (smaller than L_o or L_h), universal 3D isotropic characteristics of turbulence appear to be restored.

To confirm directly the role of these two scales, we performed numerical simulations at high resolution (2048³ points) in freely decaying turbulence at four different stratification rates and six rotating rates. We confirm the role played by L_o and L_h by considering the angular energy spectra. Moreover the two scales are associated to a change of behavior of the poloidal/toroidal components of velocity, linked to Riley's decomposition in wave/vortex mode [4], revisited using its spectral counterpart given by the Craya/Herring frame of reference in Delache et al. [5]. In addition, the latter paper has shown the evidence by DNS of a non-monotonic scale-by-scale distribution of directional anisotropy, from the smallest wave vectors (larger scales) to the Hopfinger threshold wavenumber.

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